

# Behavioral Economics

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## Lecture 5: Time Preferences

# Today's Topics

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## 1. Experiment

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2. Discounting

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3. Traditional model: exponential discounting

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6. Sophistication and Commitment

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2. Discounting
3. Traditional model: exponential discounting
4. Phenomenon: time inconsistency
5. Behavioral model: quasi-hyperbolic model
6. Sophistication and Commitment
7. Application

# Experiment

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## 2. Discounting

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- weighting future benefits and costs with present benefits and costs

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- **Problem 1**

- Receive 100 Euro now
- Receive 100 Euro in one year

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- **Problem 2**

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- **We discount the future**

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- In practice:
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  - The interest rate for borrowing is not the same as for lending money.
- And also: **why is there a positive interest rate to be earned in the market in the first place?**

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  - etc.

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- **Reason III:**
- Psychological motive: we are **impatient**.
- In this lecture, we will focus on this reason.
  - (so we assume future is certain)

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- For a consumption profile  $x_0, x_1, \dots, x_T$ :

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- Also called inter-temporal utility function

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- **Constant discounting:** in each period the same factor  $\delta$ .
- Also called **constant discounting**.

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- $\delta < 1$  implies: the sooner, the better!

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- What happens if  $\delta \in (0.87, 0.91)$ ?

# Constant Discounting

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- In Example 2, Hanneke with  $\delta > 0.75$  prefers to study today and have free tomorrow
  - She would make the same choice if the decision was shifted one week (study in one week and have free the evening in a week and one day).

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$$DU = -\delta^7 + \delta^8 \frac{4}{3} > 0 \Rightarrow \delta > 0.75$$

- In fact, the decision can be shifted to any future period  $t = \tau$  and if  $\delta > 0.75$ , she would prefer to study in  $t = \tau$  to have a free evening on  $t = \tau + 1$ .

# Constant Discounting

- **More generally:**
  - If, in period  $t = \tau$ , one prefers waiting  $s$  more weeks to get  $y$  in period  $t = \tau + s$  instead of  $x$  in period  $t = \tau$  (such that  $y > x$ ),
  - then one should also prefer waiting  $s$  more weeks now ( $t = 0$ ) to get  $y$  in period  $t = s$  instead of  $x$  now.

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- **Constant discounting implies time consistent behavior**
  - if a person prefers  $x = (x_\tau, \dots, x_T)$  to  $y = (y_\tau, \dots, y_T)$  **from the perspective of period  $t = 0$** , then she will also prefer  $x$  to  $y$  from **the perspective of period  $t = \tau$** .

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  - The person will not alter the decision in period  $\tau$  (“consistent” decision)

## Problem 3

- Receive 100 Euro now
- Receive 110 Euro in one week.

## Problem 4

- Receive 100 Euro in 4 weeks
- Receive 110 Euro in 5 weeks.

## 4. Time inconsistency

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- In **Problem 4**, people typically prefer “110 in 5 weeks” over “100 Euro in a 4 weeks”
  - This pattern of choice violates constant discounting.

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- In **Problem 4** people typically prefer “110 in 5 weeks” over “100 Euro in a 4 weeks”
  - Under exponential discounting implies  $\delta^5 u(110) > \delta^4 u(100) \Rightarrow \delta u(110) > u(100)$

# Time inconsistency

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  - Under exponential discounting implies  $u(100) > \delta u(110)$
- In **Problem 4** people typically prefer “110 in 5 weeks” over “100 Euro in a 4 weeks”
  - Under exponential discounting implies  $\delta^5 u(110) > \delta^4 u(100) \Rightarrow \delta u(110) > u(100)$
- A contradiction!

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    - In the short run people are more impatient as in the long run.
    - **“Decreasing impatience”**

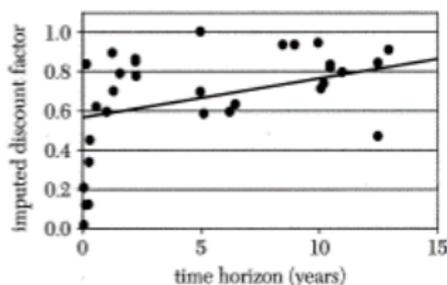


Figure 1a. Discount Factor as a Function of Time Horizon (all studies)

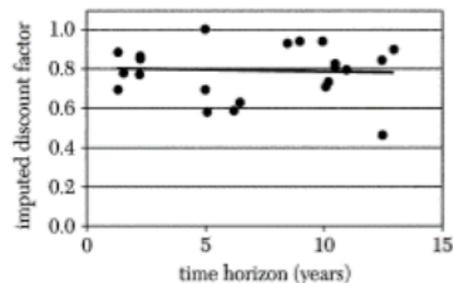


Figure 1b. Discount Factor as a Function of Time Horizon (studies with avg. horizons > 1 year)

# Empirical Findings

- Measurement and findings
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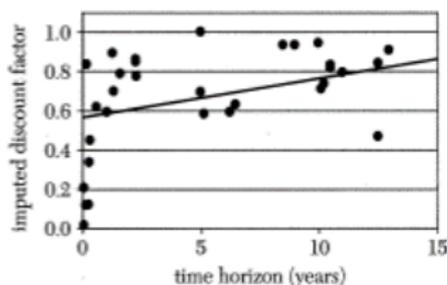


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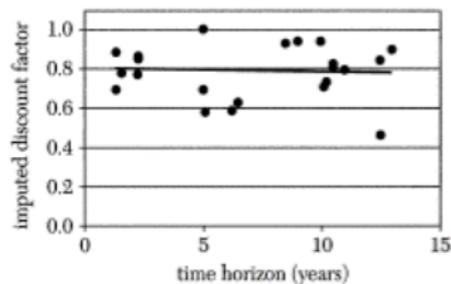


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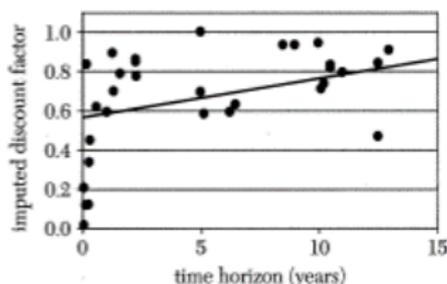


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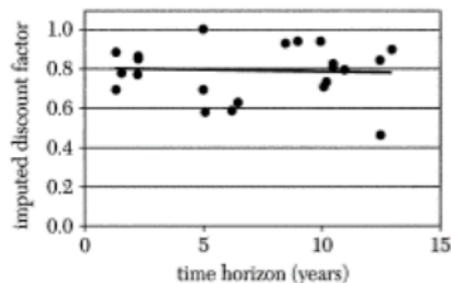


Figure 1b. Discount Factor as a Function of Time Horizon (studies with avg. horizons > 1 year)

- short-term impatience.
- violates constant discounting

# Read and van Leeuwen (1998)

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- If you were deciding **today**, would you choose fruit or chocolate for **next week**?



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- **time inconsistent preferences**

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Figure: Canonical highbrow movie

(A man seeks answers about life, death, and the existence of God as he plays chess against the Grim Reaper during the Black Death.)

## Read et al. (1999) (cont'd)

- Picking for **tonight**: 66% choose low brow.

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- time inconsistent preferences
- Intuition: Tonight I want to have fun, but next week I want things that are good for me. . .

## 5. Behavioral Model: Quasi-hyperbolic discounting.

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- if  $\beta = 1$  : **constant discounting (as before)**
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  - All future utilities are multiplied by  $\beta < 1$ .
  - $\beta$  captures the present bias.

## Quasi-hyperbolic discounting

- A consumption profile  $(x_0, x_1, \dots, x_T)$  is evaluated at  $t = 0$  as

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- Discount factor between  $t = 0$  and  $t = 1$ :  $\beta\delta$ .
- Discount factor between  $t > 0$  and  $t + 1$ :  $\delta$
- Individuals discount constantly, but not between today and tomorrow

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- **When do you write the assignment?**

Really?

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- Value of doing the assignment is the same no matter when you write it and you get the reward only after the four weeks.
- Cost of doing the assignment is not going to Feyenoord.**

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  - Reward independent on time point of writing.
  - Do the assignment in the week with the minimal cost.
- Do it this week.

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  - Perspective in two weeks: do it in three weeks.
- Do it in three weeks: **procrastination!**

## 6. Sophistication and Commitment

# Naivete vs Sophistication

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- A decision-maker with quasi-hyperbolic preferences may be aware that she is impatient.

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- A decision-maker with quasi-hyperbolic preferences may be aware that she is impatient.
- Additional parameter  $\hat{\beta}$  are the individual's beliefs about  $\beta$

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  - She does the best given future selves' correctly anticipated behavior.
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- But has correct beliefs about the future
- She solves the problem using **backward induction!**

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## Conclusion of Example 3

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- Sophistication can mitigate self-control problems.

# Commitment and Sophistication

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- Suppose that you are sophisticated and can commit at  $t = 0$  to make the assignment at any date.

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- Hence, at  $t = 0$  you commit to doing the assignment at  $t = 1$ .
- Sophisticates take advantage of commitment.

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  - Next week, the perceived discounted cost is 5.

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- Hence, you believe that the plan of doing the assignment at  $t = 0$  will happen.

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  - Next week, the perceived discounted cost is 5.
  - In two weeks, the perceived discounted cost is 8.
  - In three weeks, the perceived discounted cost is 13
- Hence, you believe that the plan of doing the assignment at  $t = 0$  will happen.
- Naives do not take advantage of commitment.

# Commitment and Sophistication

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  - Decision in the evening: setting an early wake up time at the alarm clock.
  - In the morning: snooze button

# Clocky



The screenshot displays the Stickk website interface. At the top left is the Stickk logo with the tagline "put a contract out on YOURSELF!". To the right are navigation links: Home, About Us, How To, FAQ, and Contact Us. A login box contains fields for Email and Password, with a "Login" button and a "Remember me" checkbox. Below this is a navigation bar with icons and labels for "Quit Smoking", "Exercise Regularly", "Lose Weight", and "Custom".

Below the navigation bar, a section titled "Welcome to the Quit Smoking community" includes the text: "Commitment communities are not yet available. Stickk gives you the opportunity to socialize with people who share the same goal as you. You'll have access to forums and articles written by professionals and much, much more."

A call-to-action box contains the text "You can start a commitment NOW and join the community LATER!" and a prominent orange button labeled "MAKE A COMMITMENT".

To the left of the main content is a "No Smoking" sign. To the right is a 3D illustration of a group of white figures holding hands in a circle, with one central orange figure standing with arms raised in a celebratory gesture.

Figure: "The smartest way to set and achieve your goals"

# Self-control



The screenshot shows the homepage of the SelfControl application. At the top, there is a navigation bar with links for "Overview", "Download", "FAQ", and "Code". To the right of the navigation bar are social media icons for GitHub (1.2k), Twitter (4.2M), Facebook (1.1k), and YouTube (29k). The main content area features a large black spade symbol containing a white skull and crossbones. To the right of this icon is the title "SelfControl" in a large, bold, black font. Below the title is the tagline "A free Mac application to help you avoid distracting websites." There are two buttons: a white button with a grey border labeled "View code on GitHub" and a solid blue button labeled "Download SelfControl". Below these buttons is a paragraph of text: "SelfControl is a free and open-source application for Mac OS X (10.5 or above) that lets you block **your own** access to distracting websites, your mail servers, or anything else on the Internet. Just set a period of time to block for, add sites to your blacklist, and click "Start." Until that timer expires, you will be unable to access those sites—even if you restart your computer or delete the application."

## 7. Application

# Application of commitment (Ariely and Wertenbroch, 2002)

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- **Experiment 1**
- MBA students had to submit three papers during a course.
- Two groups
  - Group A: evenly-spaced deadlines
  - Group B: set own deadlines
- The penalty for delay was 1% per day for late submission
- Demand for commitment (68%)  $\Rightarrow$  Implies sophistication

# Application of commitment (Ariely and Wertenbroch, 2002)

- No late submissions!

## Application of commitment (Ariely and Wertenbroch, 2002)

- No late submissions!
- Grades in Group A (88.7) higher than grades in Group B (85.67)

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## Application of commitment (Ariely and Wertenbroch, 2002)

- No late submissions!
- Grades in Group A (88.7) higher than grades in Group B (85.67)
  - Consistent with self-control problems
- Problem of this study: no randomization.

# Application of commitment (Ariely and Wertenbroch, 2002)

- **Experiment 2**

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- **Experiment 2**
- 21-day proofreading job: find mistakes in papers and get paid per error.
  - Group A: evenly-spaced deadlines

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  - $C > A > B$

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  - Some commitment should help ( $C > B$ )

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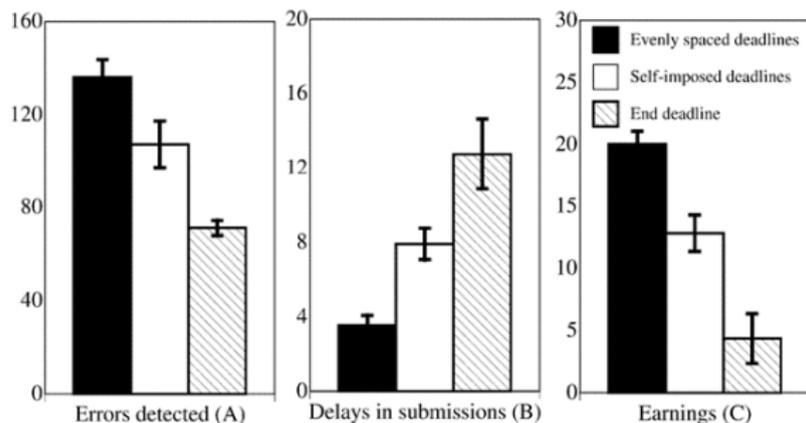


Figure: Results Ariely and Wertenbroch (2002)

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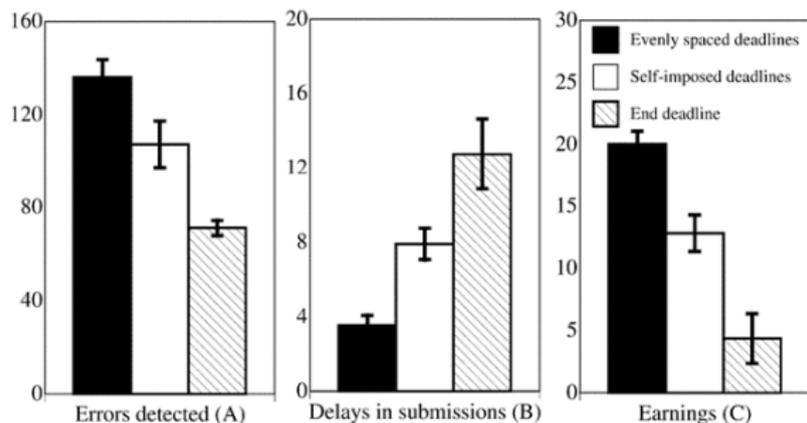


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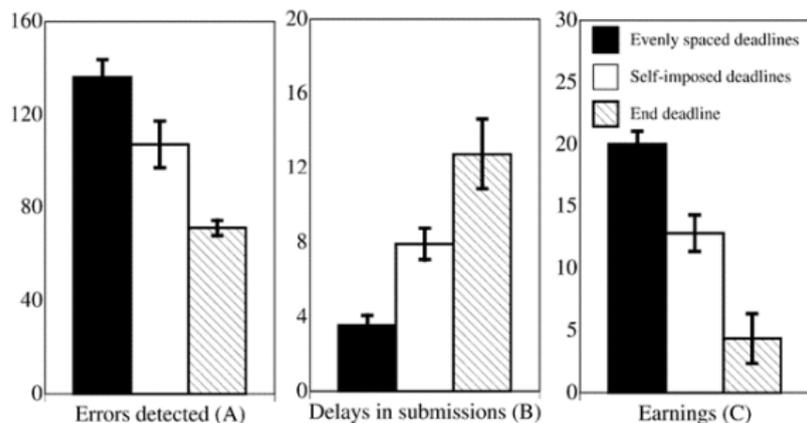


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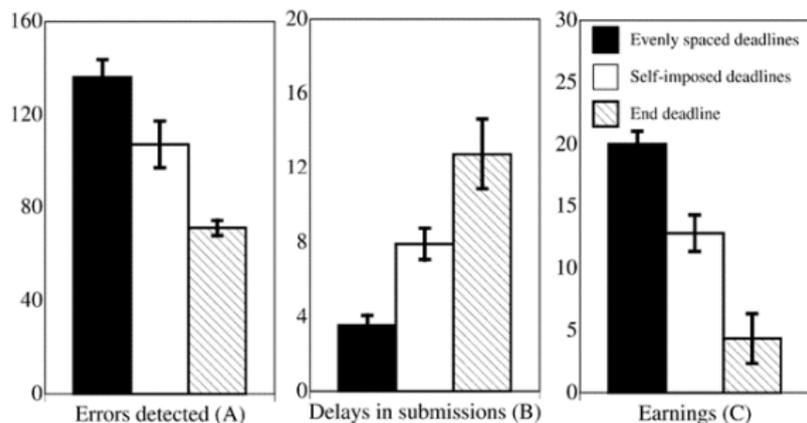


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  - People were willing to self-impose deadlines to overcome procrastination
  - Self-imposed deadlines were effective in improving task performance but were not set optimally.

## Another nice application

- Duflo, Esther, Michael Kremer, and Jonathan Robinson. “Nudging farmers to use fertilizer: Theory and experimental evidence from Kenya.” *American economic review* 101.6 (2011): 2350-2390.
- will be discussed in Lecture 9.

# Exam-like question

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- Values of going to the matches are as in Example 3, and the cost of going to each of the matches is now zero.
- **When do you go to Feyenoord?**

The End!

# Today's recommendation

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- Slipknot's "We are not your kind" (2019).
- **Interesting economics fact:** Slipknot received a \$500,000, seven-album deal, from Roadrunner Records; the band signed the deal publicly on July 8, 1998. (Talking about present bias)